## Section 7.1 -- Circles

## **Definitions:**

Circle: the set of all points in the same plane that are a fixed distance from a point called

its center

Radius: a line segment drawn from the center of a circle to one of the points on the circle

*Chord:* a line segment connecting two points on a circle

Diameter: a chord that passes through the center of a circle

Tangent: a line that has exactly one point of intersection with a circle

*Point of Tangency:* the point of intersection between a circle and a tangent

*Arc:* a continuous portion of a circle

Semicircle: an arc of a circle whose endpoints are endpoints of a diameter of a circle

Major Arc: an arc that is greater than a semicircle

Minor Arc: an arc that is less than a semicircle

Congruent Circles: two or more circles with congruent radii

Central Angle: an angle whose vertex is at the center of a circle and whose sides are radii

of the circle

Measure of an Arc: equal to the number of degrees in the central angle that intercepts the arc

Congruent Arcs: two arcs in the same circle or congruent circles that have the same

measure

Definition of Betweenness for Arcs: If A, B, and C are three points on the same arc, and B is

between A and C, then  $\widehat{mAC} = \widehat{mAB} + \widehat{mBC}$  or any equivalent statement.

Inscribed Angle: an angle whose vertex is on a circle and whose sides are chords of the

circle

Secant: a line that intersects a circle in two points

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## **Postulates and Theorems:**

From defn. of circle: All radii of the same circle are congruent.

Theorem: The length of a diameter of a circle is twice the length of any of its radii.

Postulate: A line drawn from the center of a circle to a point of tangency is perpendicular to

the tangent that passes through the point of tangency.

Postulate: If a line is perpendicular to a radius at the point where the radius intersects a

circle, then the line is tangent to the circle.

Theorem: Two circles are congruent if and only if their diameters are congruent.

Theorem: The measure of an inscribed angle is equal to  $\frac{1}{2}$  the measure of its intercepted arc.

Theorem: The measure of an angle formed by a tangent and a chord is equal to  $\frac{1}{2}$  the

measure of its intercepted arc.

Theorem: If two chords intersect within a circle, the measure of each angle formed is equal

to ½ the sum of the measures of its intercepted arc and the intercepted arc of its

vertical angle.

Theorem: The measure of an angle formed by the intersection of two secants outside a circle

is equal to  $\frac{1}{2}$  the difference of the measures of the intercepted arcs.

Theorem: The measure of an angle formed by the intersection of a tangent and a secant

outside a circle is equal to ½ the difference of the measures of the intercepted

arcs.