Two Measures of Variation:

1. Range - difference between the largest number and smallest number
2. Standard Deviation - a measure of the variation from the mean
a. Population Standard Deviation
b. Sample Standard Deviation

Example 1: For this set of numbers-

$$
\begin{array}{llllllll}
7 & 9 & 18 & 22 & 27 & 29 & 32 & 40
\end{array}
$$

a) Find the Range
b) Find the Standard Deviation

Variance: $s^{2}=\frac{\sum(X-\bar{X})^{2}}{n-1}$

Standard Deviation is the square root of the variance.
$s=\sqrt{\frac{\sum(X-\bar{X})^{2}}{n-1}}$

Example 2: Find the Standard Deviation for this grouped data.

| Interval | Frequency |
| :--- | :--- |
| $20-24$ | 3 |
| $25-29$ | 2 |
| $30-34$ | 4 |
| $35-39$ | 1 |

Standard Deviation for a Grouped Distribution:

$$
s=\sqrt{\frac{\sum f(X-\bar{X})^{2}}{n-1}}
$$

NOTE: Group Standard Deviation formula is calculated differently from textbook so answers may vary slightly from what is in text.

Chebyshev's Theorem:
For any distribution of numerical data, at least
$1-\frac{1}{k^{2}}$ of the numbers lie within k standard deviations of the mean.

